

# The Core of $^{25}\text{F}$ in the rotational model

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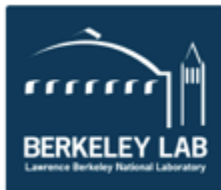


ORNL PHYSICS DIVISION

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Seminar

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**ENERGY**

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Science

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# Outline

Short introduction

Shell Model and residual interactions

Deformation and the Nilsson Model

Particle Rotor Model 101

Application to  $^{29}\text{F}$

The structure of  $^{25}\text{F}$  and its core

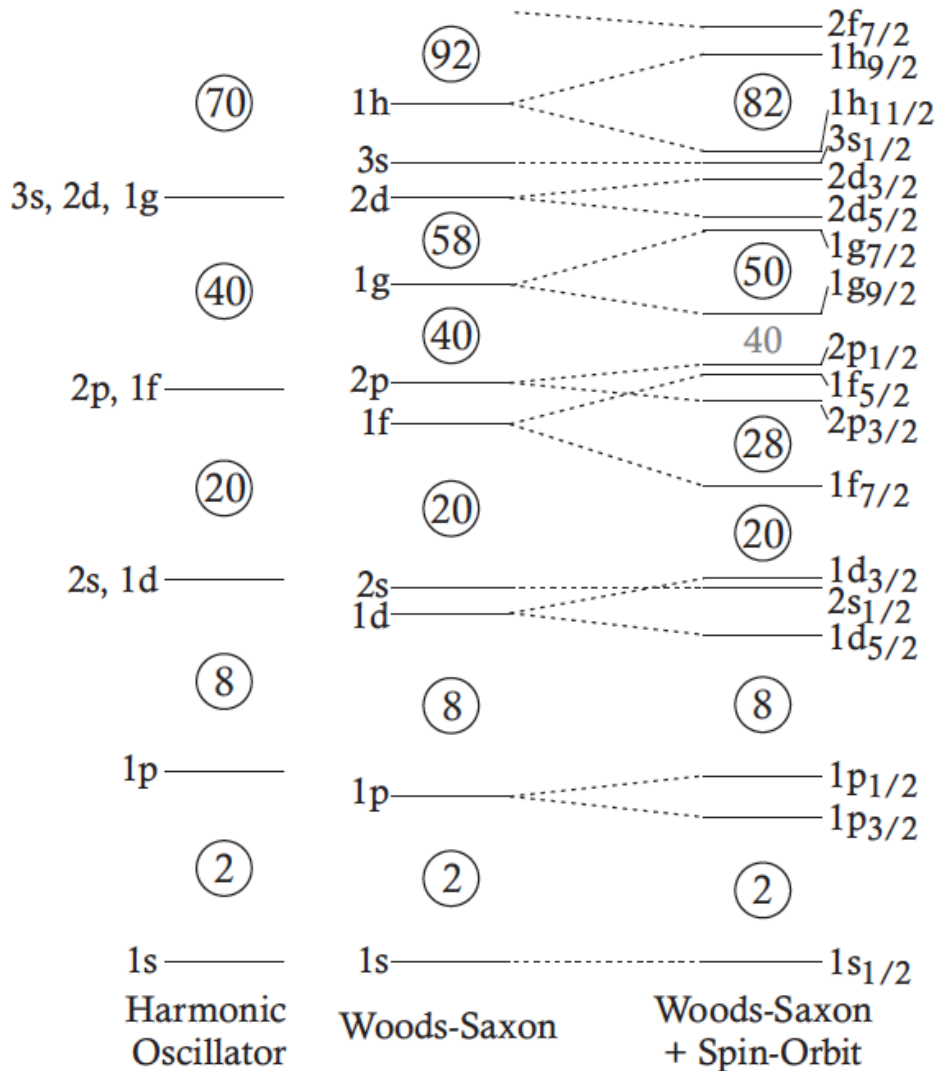
RIBF (p,2p) studies

NSCL p-KO

The PRM view

Summary and Conclusions

# Nuclear Shell Model



Maria Goeppert-Mayer &  
Hans D. Jensen  
1963

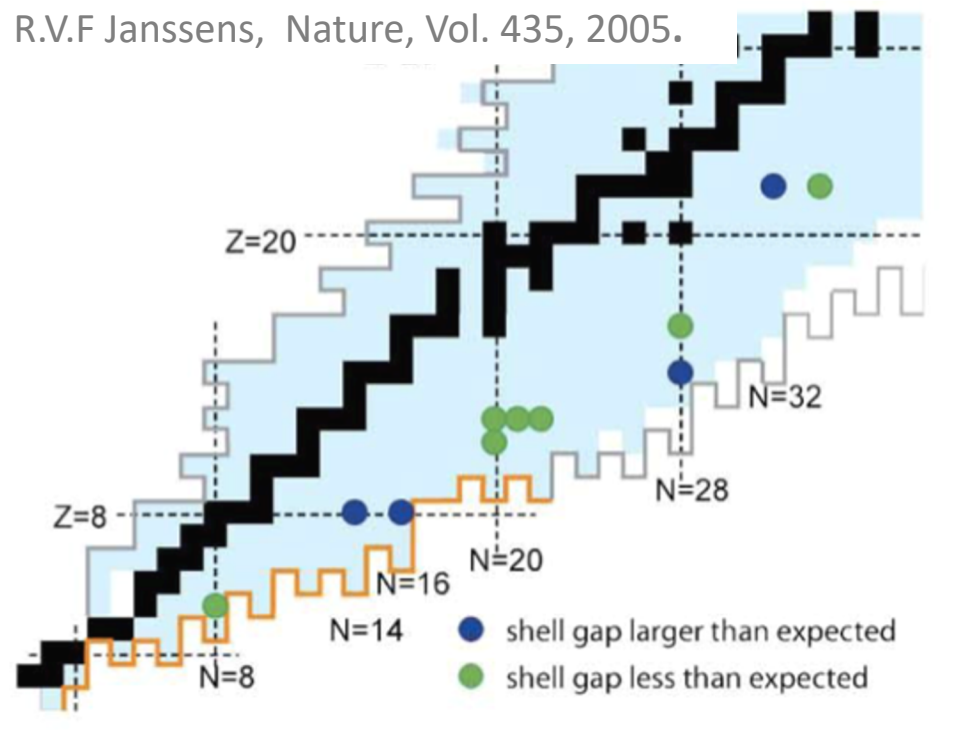
Maria Goeppert-Mayer, Phys. Rev. **75**, 1969 (1949).  
O. Haxel, Phys. Rev. **75**, 1766 (1949).

# Evolution of Shell Structure and Collectivity

“Classic” magic numbers are generally correct only for stable and near stable isotopes

Experimental studies of new exotic isotopes revealed changes in shell structure and collectivity, and provided insight on the important role played by the central, tensor, (and 3N) forces in these changes

R.V.F Janssens, Nature, Vol. 435, 2005.



A. Poves and J. Retamosa, Phys. Lett. B 184, 311 (1987).

E.K. Warburton, J.A. Becker and B.A. Brown, Phys. Rev. C 41, 1147 (1990).

T. Otsuka *et al.*, Phys. Rev. Lett. **87**, 082502 (2001).

O. Sorlin and M. Porquet, Prog. Part.Nucl. Phys. **61**, 602 (2008).

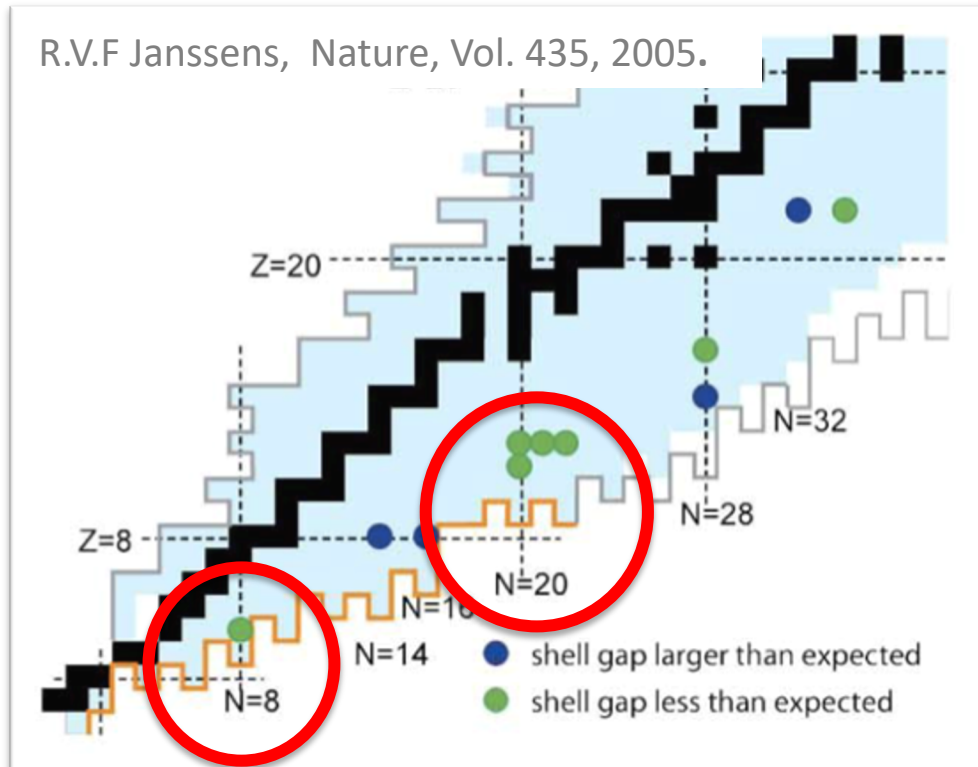
K. Heyde and J. L. Wood, Rev. Mod. Phys. **83**, 1467 (2011).\*

T. Otsuka, A. Gade and O. Sorlin, Rev. Mod. Phys.,92(2020)

# Evolution of Shell Structure and Collectivity

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Experimental studies of new exotic isotopes revealed changes in shell structure and collectivity, and provided insight on the important role played by the central, tensor, (and  $3N$ ) forces in these changes



**Much evidence has been obtained for the existence of deformed ground states, and a good understanding of the physical mechanism behind the inversion.**

# The effective interaction between nucleons deduced from nuclear spectra\*

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*University of California, Davis, California 95616*

**I.B:**  
**I.D.1**

*Nuclear Physics A239 (1975) 45–73; © North-Holland Publishing Co., Amsterdam*

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## EFFECTIVE TWO-BODY INTERACTION IN SIMPLE NUCLEAR SPECTRA

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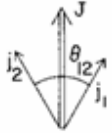
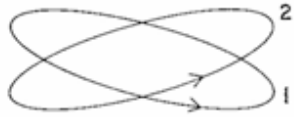
H. A. BETHE

*Laboratory of Nuclear Studies, Cornell University, Ithaca, New York, 14850*

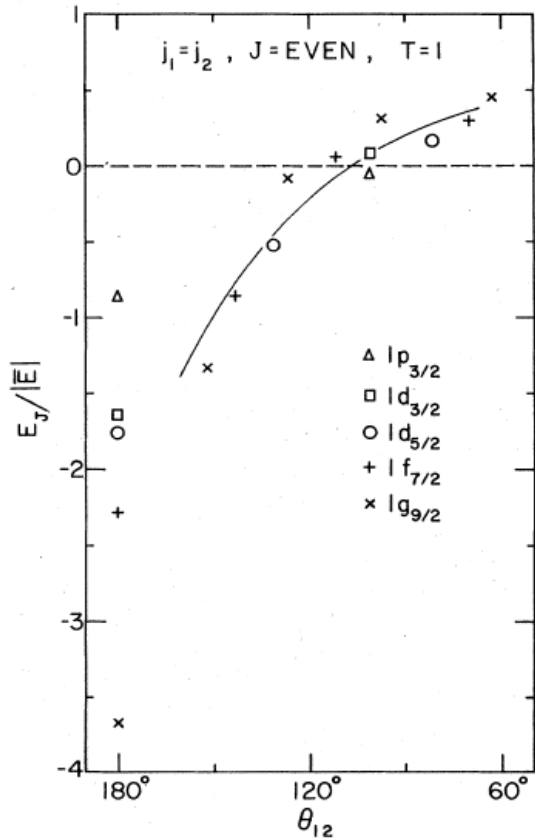
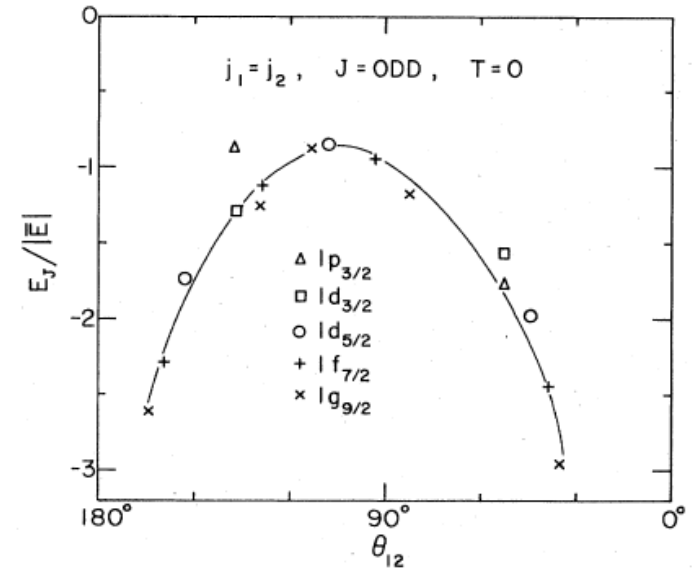
and

W. M. ALBERICO

*Istituto di Fisica Teorica dell'Università di Torino, Torino, Italy*



$$\theta_{12} = \cos^{-1} \frac{j_1(j_1+1) + j_2(j_2+1) - J(J+1)}{[2j_1j_2(j_1+1)(j_2+1)]^{1/2}}$$



$$V(1,2) \approx \underbrace{G\delta(\theta_{12})}_{\text{Short-range (Pairing)}} + \underbrace{V_2 P_2(\theta_{12})}_{\text{long-range (Quadrupole)}}$$

Short-range (Pairing) + long-range (Quadrupole)

$$G \approx 20 \text{ MeV} / A$$

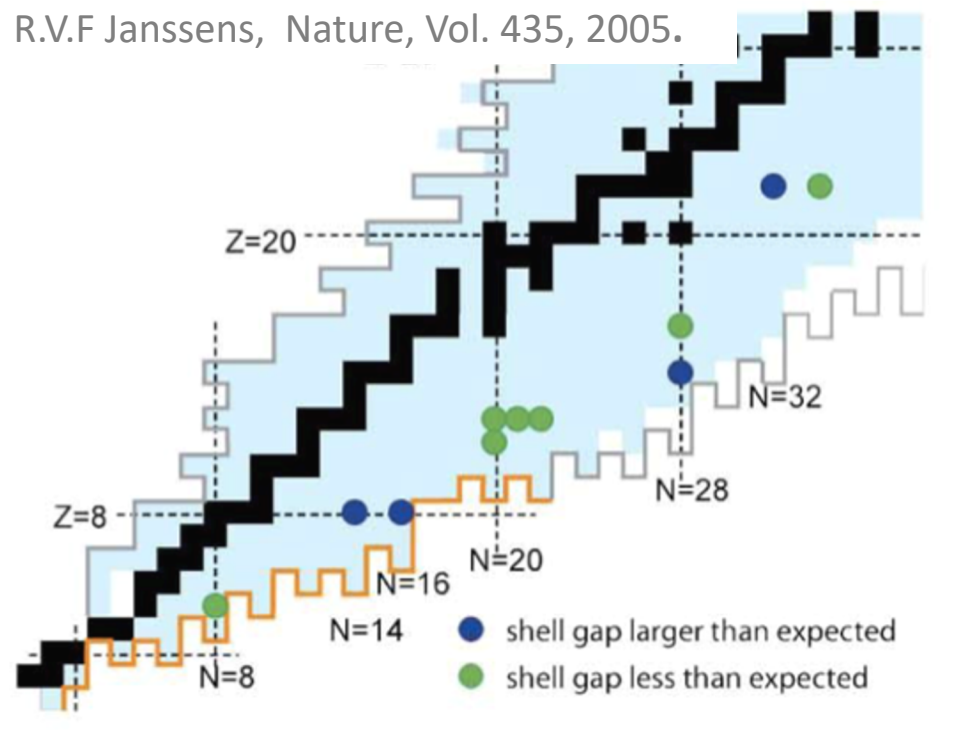
$$V_2 \approx 50 \text{ MeV} / A$$

# Evolution of Shell Structure and Collectivity

“Classic” magic numbers are generally correct only for stable and near stable isotopes

Experimental studies of new exotic isotopes revealed changes in shell structure and collectivity, and provided insight on the important role played by the central, tensor, (and 3N) forces in these changes

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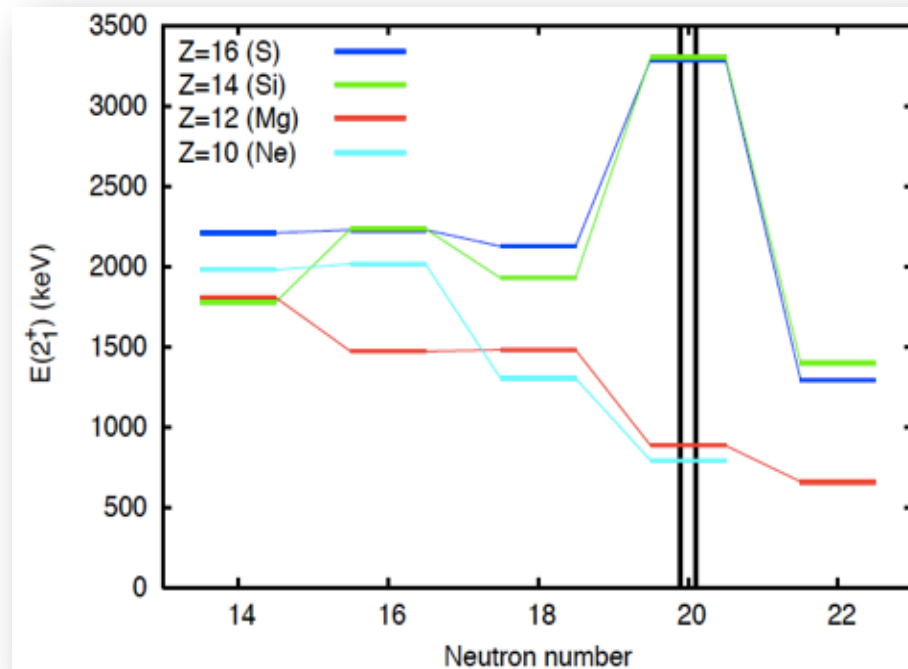


For many body configurations the **single-particle energy scale** plays a major role

A delicate balance between the **monopole field** and correlations.

$$H = E_{sp} + GP^{\dagger}P + xQ.Q$$

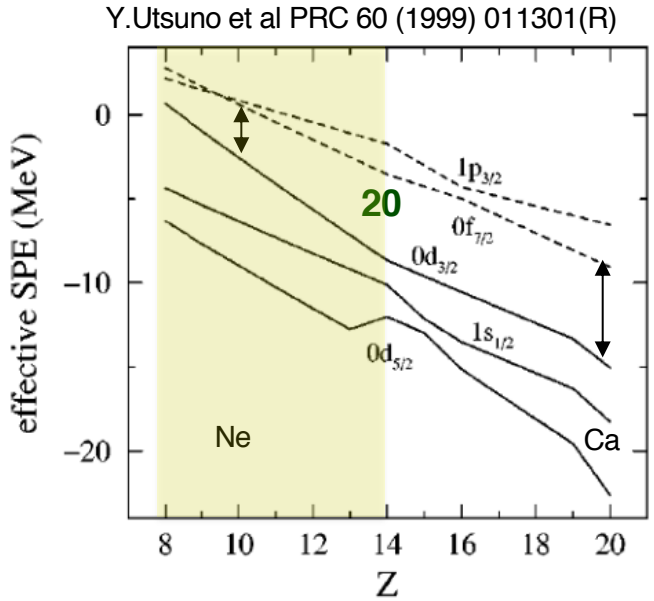
## N=20 shell gap



A. Poves and J. Retamosa, [Phys. Lett. B](#) **184**, 311 (1987).

E. K. Warburton, J. A. Becker, and B. A. Brown, [Phys. Rev. C](#) **41**, 1147 (1990).

N=20 shell gap



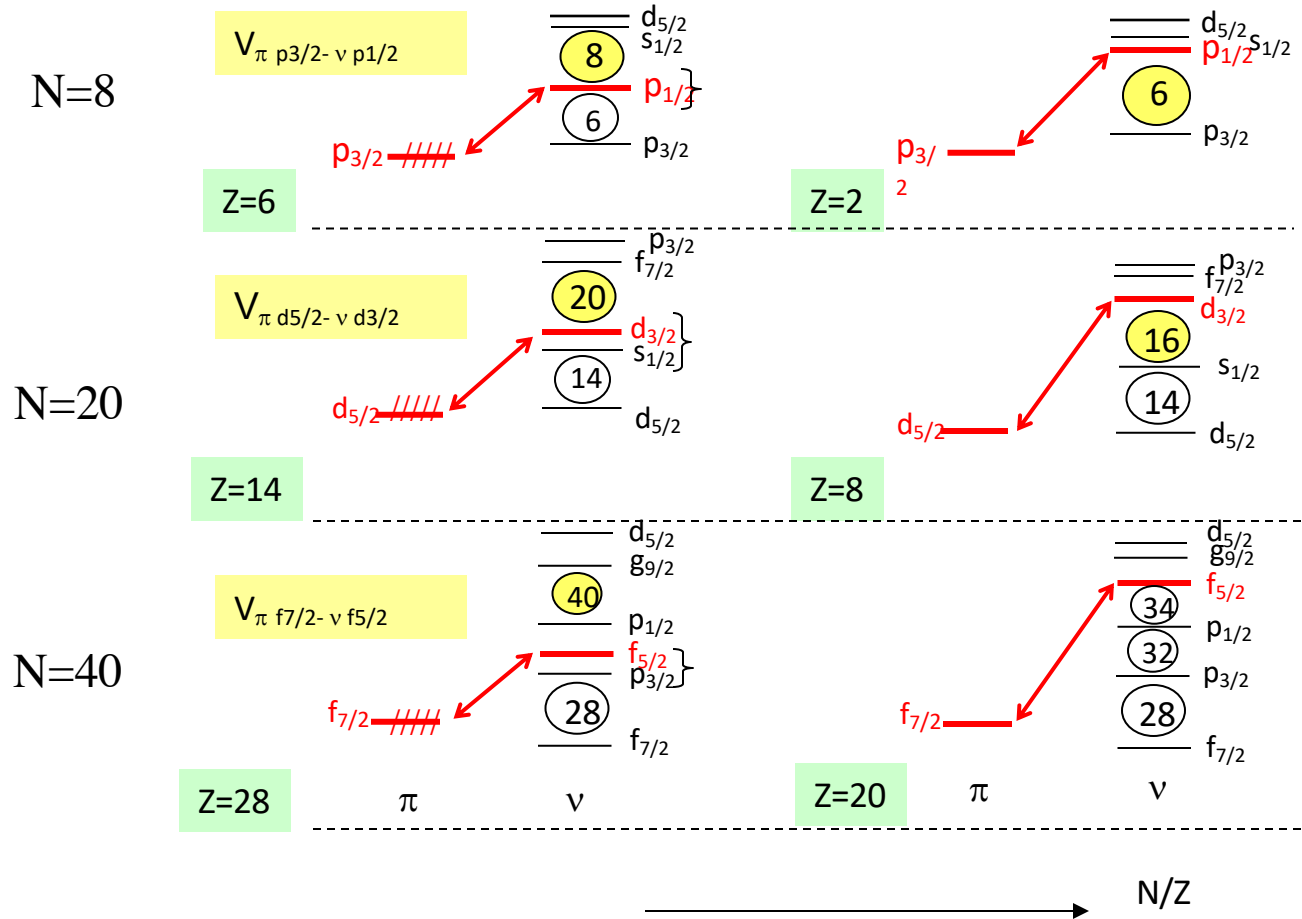
Role of the  $\pi d_{5/2} - \nu d_{3/2}$  interaction

$\Delta l = \Delta j = 2$   
 $\rightarrow$  Quadrupole Correlations

$d_{5/2} \quad | \quad s_{1/2} \quad | \quad d_{3/2}$

$$H = Esp + GP^+P + xQ.Q$$

# Harmonic Oscillator Shell Closures



How about the deformed shell model ?

# Nilsson Model



- Anisotropic harmonic oscillator potential

$$V(r) = \frac{1}{2} m (\omega_1^2 x^2 + \omega_2^2 y^2 + \omega_3^2 z^2) - \mathbf{C} \cdot \mathbf{l} \cdot \mathbf{s} - D l^2$$

- If axial symmetry is presumed:  $\omega_1 = \omega_2 \neq \omega_3$
- An elongation parameter,  $\varepsilon$ , is introduced such that:

$$\omega_3 = \omega_0 \left( 1 - \frac{2}{3} \varepsilon \right) \quad \omega_1 = \omega_2 = \omega_0 \left( 1 + \frac{1}{3} \varepsilon \right) \quad \varepsilon = \frac{(\omega_1 - \omega_3)}{\omega_0}$$

- Without spin-orbit and  $l^2$  term the Nilsson energy levels are given by:

$$E = \hbar \omega_1 \left( n_1 + \frac{1}{2} \right) + \hbar \omega_2 \left( n_2 + \frac{1}{2} \right) + \hbar \omega_3 \left( n_3 + \frac{1}{2} \right) = \hbar \omega_0 \left[ \left( N + \frac{3}{2} \right) - \varepsilon \left( n_3 - \frac{N}{3} \right) \right]$$

- In addition to the principal oscillator number  $N$  and its component  $n_3$  the Nilsson quantum numbers are  $\Lambda = l_z$ ,  $\Sigma = s_z$ ,  $\Omega = \Lambda + \Sigma = j_z$  and parity  $\pi = (-1)^l$ .
- Nilsson levels are labeled:  $[N n_3 \Lambda] \Omega^\pi$

# Nilsson Diagram

- The effects of deformation can be seen in the diagram.

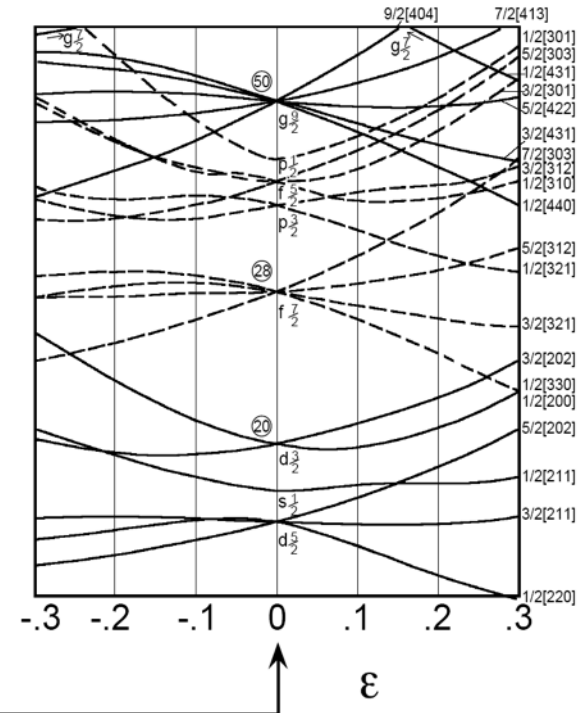
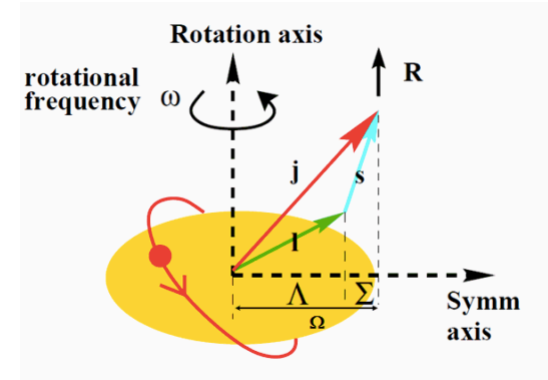
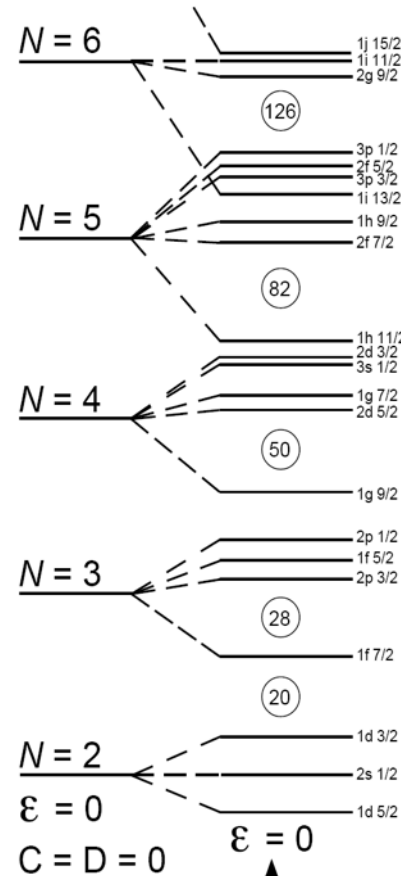
- Each spherical level labeled by  $N(l_j)$  at  $\epsilon=0$ , is split into  $(2j+1)/2$  levels with

$$\Omega = \pm \frac{1}{2}, \pm \frac{3}{2}, \dots, \pm j.$$

- The remaining degeneracy means that each level can accommodate two nucleons.

- Orbits with lower  $\Omega$  are shifted downwards for  $\epsilon > 0$  (prolate) and upwards for  $\epsilon < 0$  (oblate).

$$\chi_\nu = \sum_{\alpha j \Omega} c_{\alpha j \Omega}^{(\nu)} \psi_{\Omega}^{\alpha j}, \quad \alpha = N, l.$$



Deformed Mean Field

## Coriolis effects and rotation alignment in nuclei\*†

F. S. Stephens

*Lawrence Berkeley Laboratory, University of California, Berkeley, California 94720*

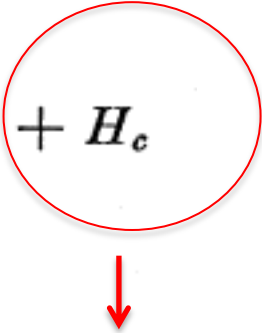


$$E_{\text{Cor}}(\text{max}) \approx 2(\hbar^2/2J)Ij.$$

## The Particle plus Rotor Hamiltonian

$$\begin{aligned} H &= H_p + H_{\text{rot}} = H_p + (\hbar^2/2\mathcal{I})\mathbf{R}^2 \\ &= H_p + (\hbar^2/2\mathcal{I})(R_x^2 + R_y^2), \end{aligned}$$

$$\begin{aligned} H &= H_p + (\hbar^2/2\mathcal{I})[I(I+1) - K^2] + H_c \\ &+ (\hbar^2/2\mathcal{I})[\langle \mathbf{j}^2 \rangle - \Omega^2], \end{aligned}$$

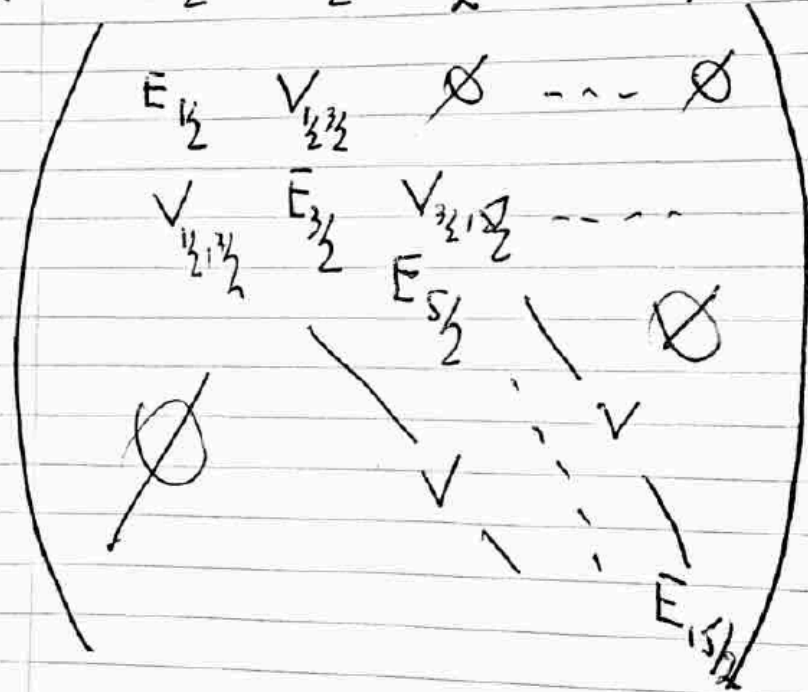

$$\begin{aligned} H_c &= -2(\hbar^2/2\mathcal{I})[I_x j_x + I_y j_y] \\ &= -(\hbar^2/2\mathcal{I})[I_+ j_- + I_- j_+]. \end{aligned}$$

$$\begin{aligned} \langle I, \Omega \pm 1 | H_c | I, \Omega \rangle \\ = -(\hbar^2/2\mathcal{I})[(I \mp K)(I \pm K + 1)]^{1/2} \langle \Omega \pm 1 | j_{\pm} | \Omega \rangle, \end{aligned}$$

$$\langle j, \Omega \pm 1 | j_{\pm} | j, \Omega \rangle = [(j \mp \Omega)(j \pm \Omega + 1)]^{1/2}.$$

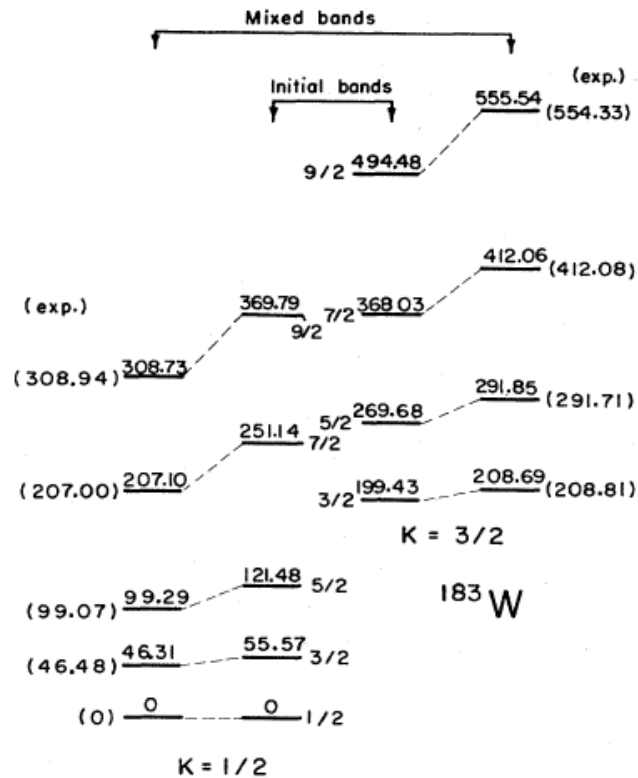
# IRM Matrix

$$K = \Omega \quad 1/2 \quad 3/2 \quad 5/2 \quad \dots \quad 15/2$$



$$\psi_I = \sum_K \mathcal{A}_K |IK\rangle.$$

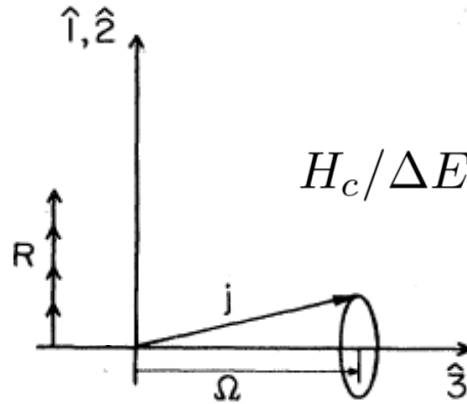
# The first study



Kerman, A. K., 1956, Dan. Mat. Fys. Medd. 30, No. 15.

# Coupling Limits

Deformation aligned  
Strongly coupled

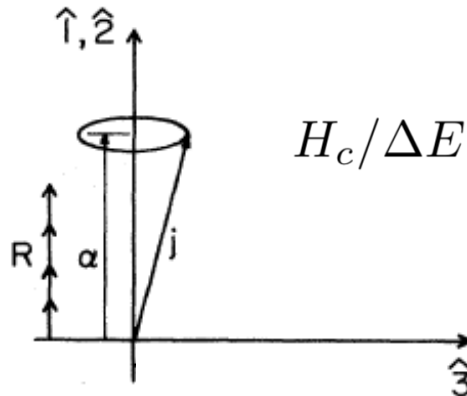


$$H_c/\Delta E \ll 1$$

$$I = K, K+1, \dots$$

$$E(K, I) = E_K + AI(I+1) + BI^2(I+1)^2 + \dots$$

Rotation aligned  
Decoupled



$$H_c/\Delta E \gg 1$$

$$I = j, j+2, j+4, \dots$$

$$E(I+2) - E(I) \approx E(R+2) - E(R).$$

# Structure of $^{29}\text{F}$

PHYSICAL REVIEW C **95**, 041301(R) (2017)

## Low- $Z$ shore of the “island of inversion” and the reduced neutron magicity toward $^{28}\text{O}$

P. Doornenbal,<sup>1,\*</sup> H. Scheit,<sup>1,2,†</sup> S. Takeuchi (武内 聡),<sup>1,‡</sup> Y. Utsuno (宇都野 穰),<sup>3</sup> N. Aoi (青井 考),<sup>1,§</sup> K. Li (李 闊昂),<sup>1,2</sup> M. Matsushita (松下 昌史),<sup>1,4,||</sup> D. Steppenbeck,<sup>1</sup> H. Wang (王 赫),<sup>1,2</sup> H. Baba (馬場 秀忠),<sup>1</sup> E. Ideguchi (井手口 栄治),<sup>5,§</sup> N. Kobayashi (小林 信之),<sup>6,§</sup> Y. Kondo (近藤 洋介),<sup>6</sup> J. Lee (李 曉菁),<sup>1,¶</sup> S. Michimasa (道正 新一郎),<sup>5</sup> T. Motobayashi (本林 透),<sup>1</sup> T. Otsuka (大塚 孝治),<sup>5,7</sup> H. Sakurai (櫻井 博儀),<sup>1</sup> M. Takechi (武智 麻耶),<sup>1,#</sup> Y. Togano (桐野 泰宏),<sup>1,‡</sup> and K. Yoneda (米田健一郎)<sup>1</sup>

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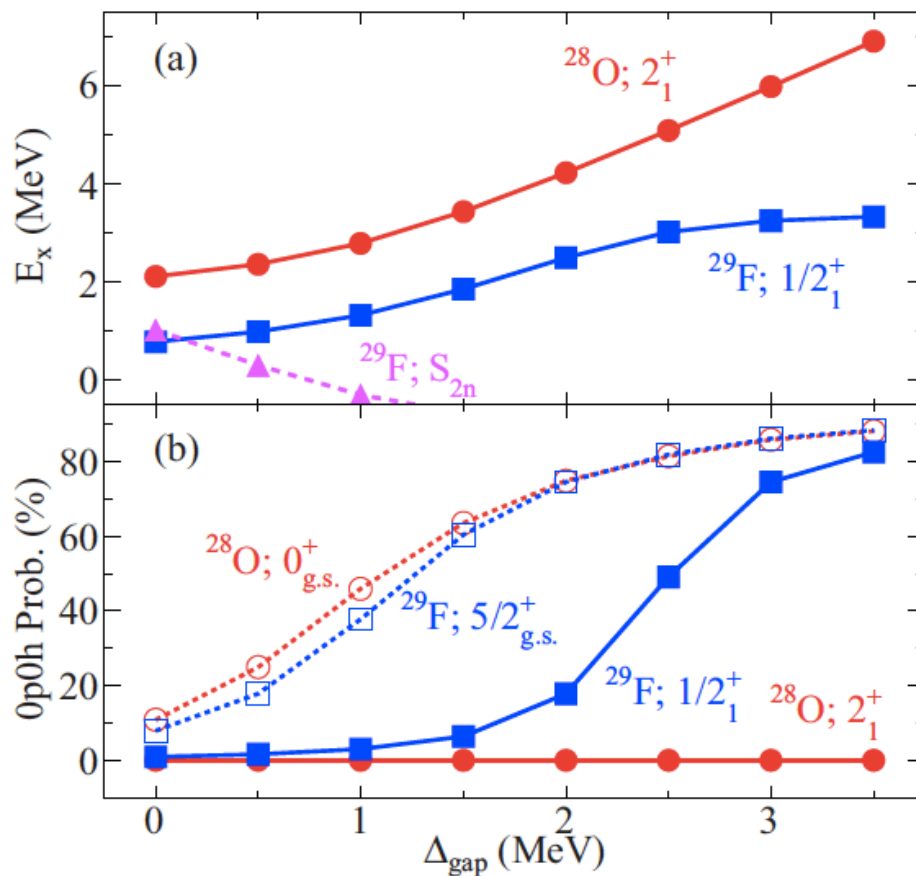
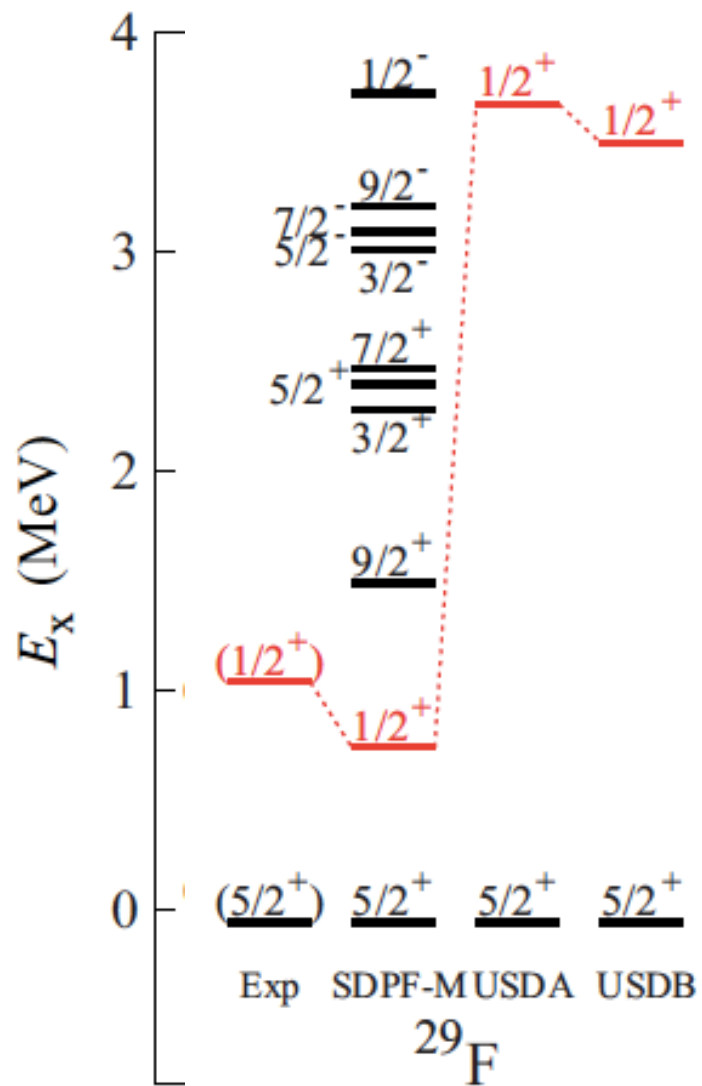
<sup>6</sup>Department of Physics, Tokyo Institute of Technology, Meguro, Tokyo 152-8551, Japan

<sup>7</sup>Department of Physics, University of Tokyo, Bunkyo, Tokyo 113-0033, Japan

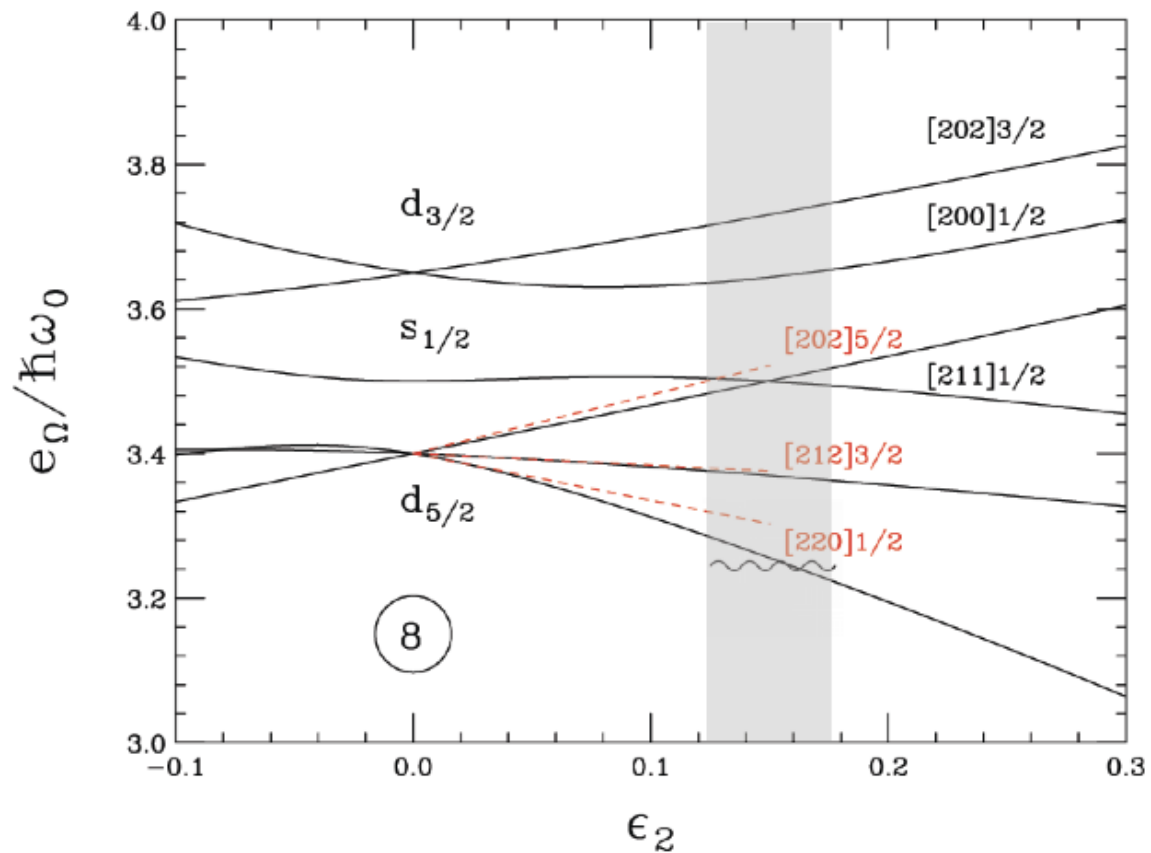
(Received 11 February 2015; revised manuscript received 20 February 2017; published 13 April 2017)

The two odd-even fluorine isotopes  $^{27,29}\text{F}$  were studied via in-beam  $\gamma$ -ray spectroscopy at the RIKEN Radioactive Isotope Beam Factory. A secondary beam of  $^{30}\text{Ne}$  was used to induce one-proton and one-proton–two-neutron removal reactions on carbon and polyethylene targets at midtarget energies of 228 MeV/ $u$ . Excited states were observed at 915(12) keV for  $^{27}\text{F}$  and at 1080(18) keV for  $^{29}\text{F}$ . Both were assigned a  $1/2_1^+$  spin and parity. The low transition energy for  $^{29}\text{F}$  largely disagrees with shell model predictions restricted to the  $sd$  model space. Calculations using effective interactions that include the neutron  $pf$  shell indicate that the  $N = 20$  gap is quenched for  $^{29}\text{F}$ , thus extending the “island of inversion” to isotopes with proton number  $Z = 9$ . Variations of the  $N = 20$  gap further reveal a strong correlation to the  $1/2_1^+$  level energy in  $^{29}\text{F}$  and suggest a persistent reduced neutron gap for  $^{28}\text{O}$ .

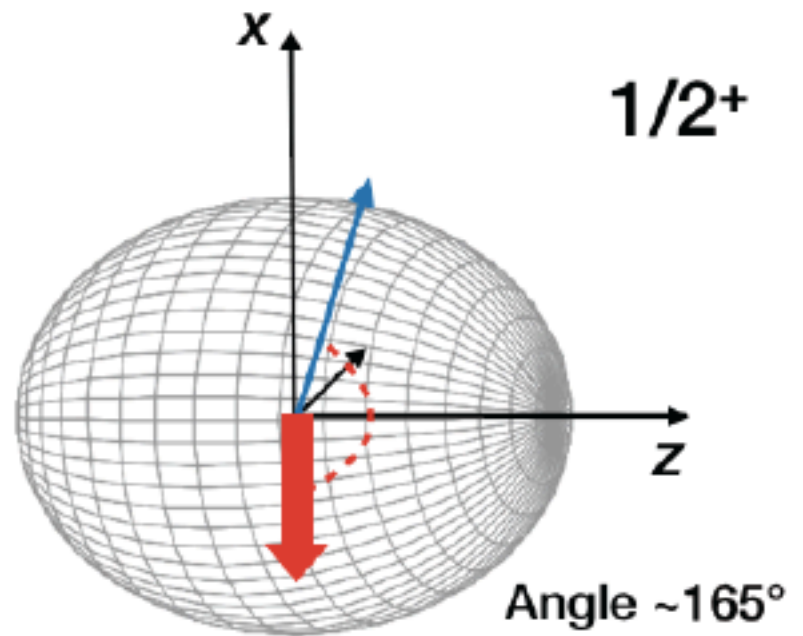
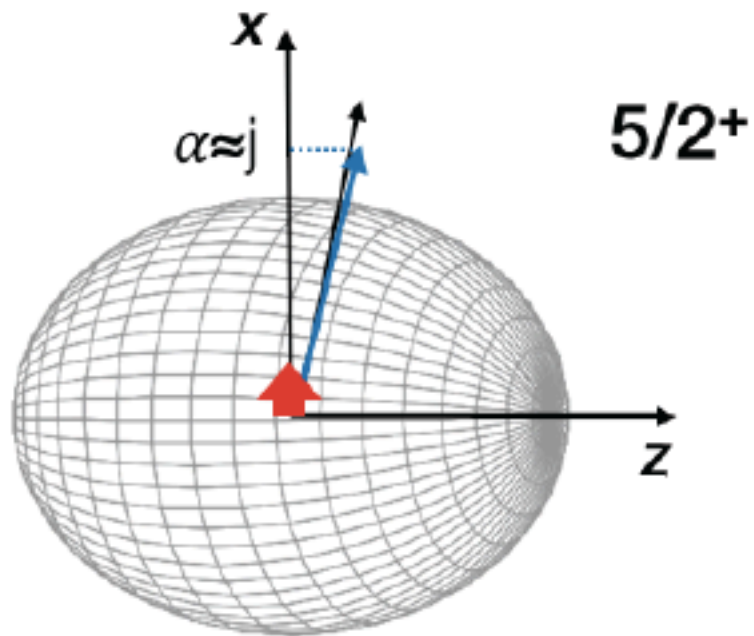
# Structure of $^{29}\text{F}$



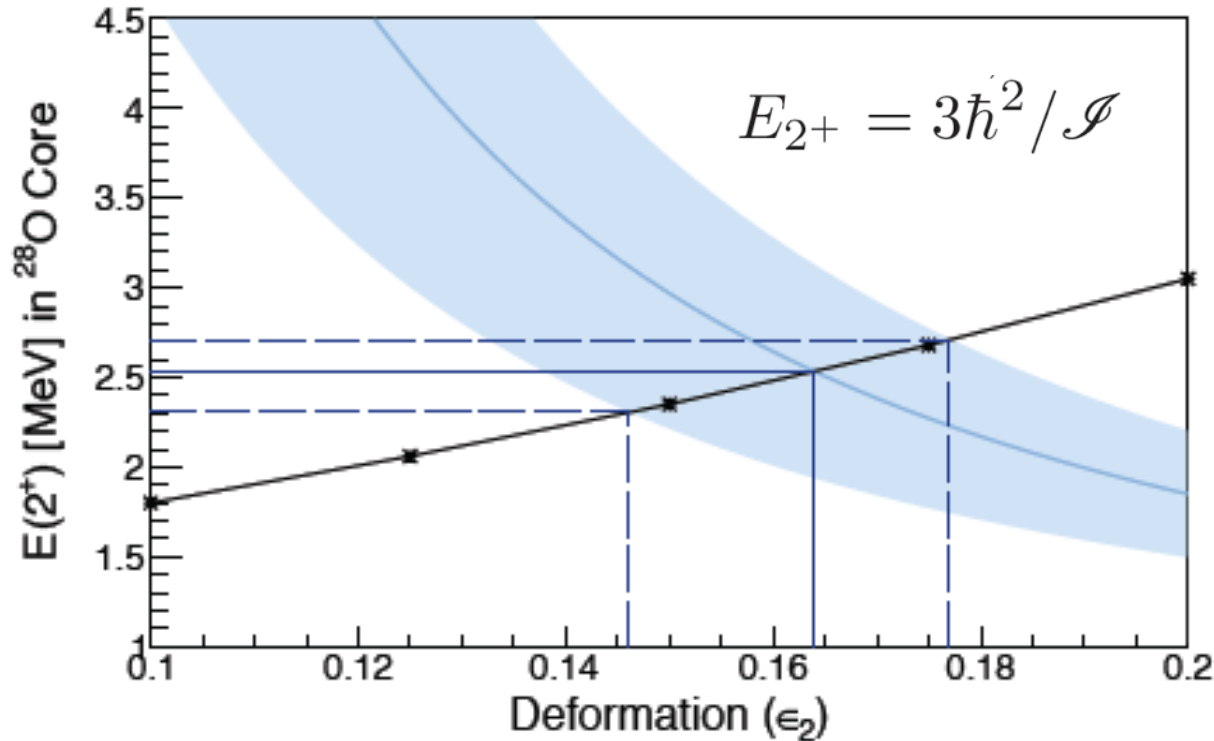
# The Nilsson view



# Structure of $^{29}\text{F}$ : Geometry



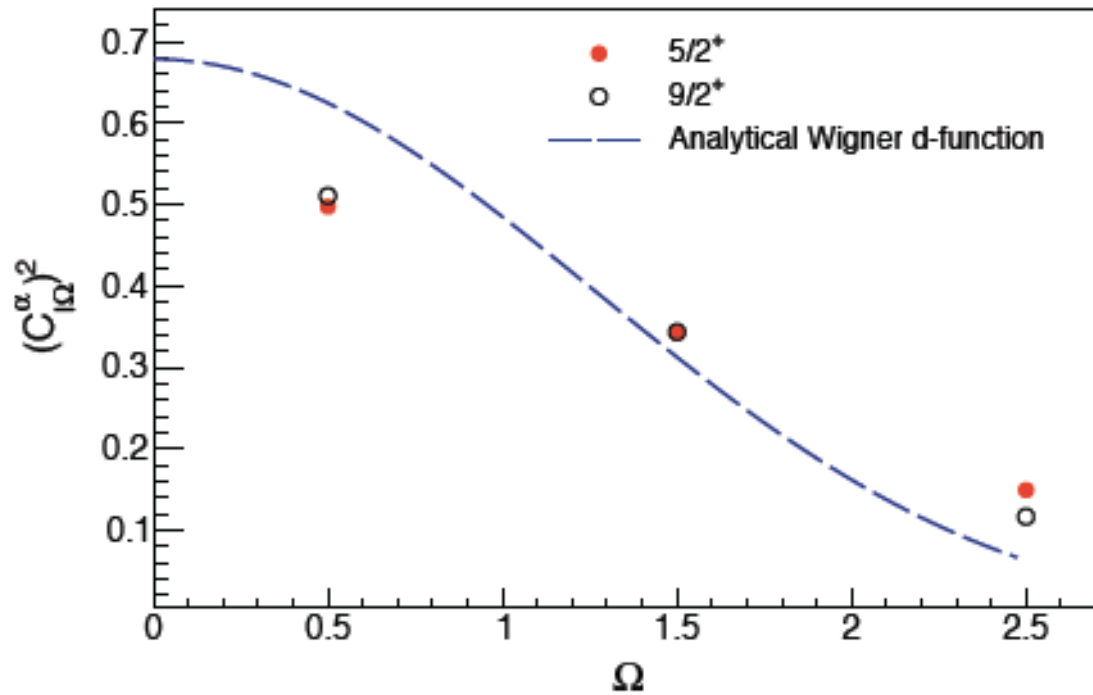
# Structure of $^{29}\text{F}$ : PRM Solution



PRM

$$\mathcal{I} = \frac{\mathcal{I}_{rigid}}{\left(1 + \left(\frac{2\Delta}{\hbar\omega_0\epsilon_2}\right)^2\right)^{3/2}}$$

# Structure of $^{29}\text{F}$ : Decoupled Band



$$|I, \alpha\rangle = \sum_{\Omega_p=1/2}^{5/2} C_{I\Omega_p}^\alpha |I, \Omega_p\rangle$$

$$C_{I\Omega}^\alpha \approx d_{\alpha,\Omega}^j(\pi/2)$$

# Direct reactions

$$d\sigma^{(-1)}(j; I_1 \rightarrow I_2) = (2I_1 + 1)^{-1} \sum_{M_1 M_2 m} d\sigma^{(-1)}(jm; I_1 M_1 \rightarrow I_2 M_2)$$

$$= (2j + 1)^{-1} (2I_1 + 1)^{-1} \langle I_1 || a^\dagger(j) || I_2 \rangle^2 d\sigma_{\text{sp}}^{(-1)}(j)$$

$$d\sigma_{\text{sp}}^{(-1)}(j) = \sum_m d\sigma_{\text{sp}}^{(-1)}(jm)$$



Reaction  
DWBA  
Eikonal  
DWIA



Structure

$$\mathcal{S} = (2I_2 + 1)^{-1} \langle I_2 || a^\dagger(j) || I_1 \rangle^2$$

# Direct reactions

## Sum rules

$$\begin{aligned}\sum_{\alpha I_2} \langle I_1 \| a^\dagger(j) \| \alpha I_2 \rangle^2 &= (2I_1 + 1) \langle I_1 M_1 | \sum_m a^\dagger(jm) a(jm) | I_1 M_1 \rangle \\ &= (2I_1 + 1) n(j)\end{aligned}$$

$$\begin{aligned}\sum_{\alpha I_2} \langle \alpha I_2 \| a^\dagger(j) \| I_1 \rangle^2 &= (2I_1 + 1) \langle I_1 M_1 | \sum_m a(jm) a^\dagger(jm) | I_1 M_1 \rangle \\ &= (2I_1 + 1)(2j + 1 - n(j))\end{aligned}$$

## How Different is the Core of $^{25}\text{F}$ from $^{24}\text{O}_{\text{g.s.}}$ ?

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Evidence for a doubly magic  $^{24}\text{O}$ 

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NSCL  
MoNA

$^{26}\text{F}$  85 MeV/A

PRL **102**, 152501 (2009)

PHYSICAL REVIEW LETTERS

week ending  
17 APRIL 2009

One-Neutron Removal Measurement Reveals  $^{24}\text{O}$  as a New Doubly Magic Nucleus

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GSF FRS

$^{24}\text{O}$  at 920 MeV/A

PRL **109**, 022501 (2012)

PHYSICAL REVIEW LETTERS

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13 JULY 2012

 $N = 16$  Spherical Shell Closure in  $^{24}\text{O}$ 

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RIKEN

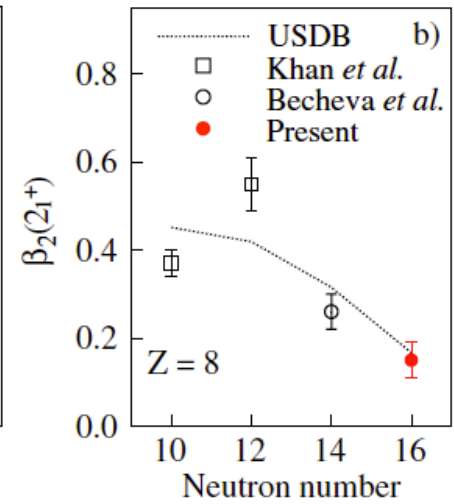
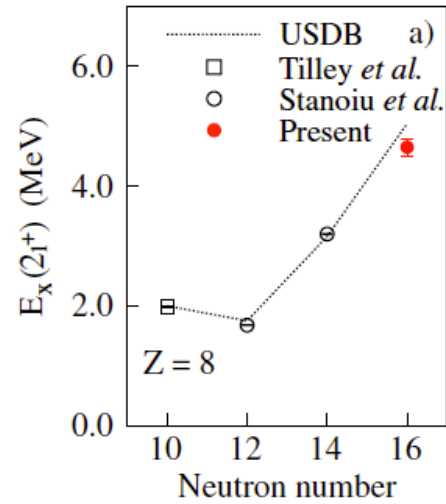
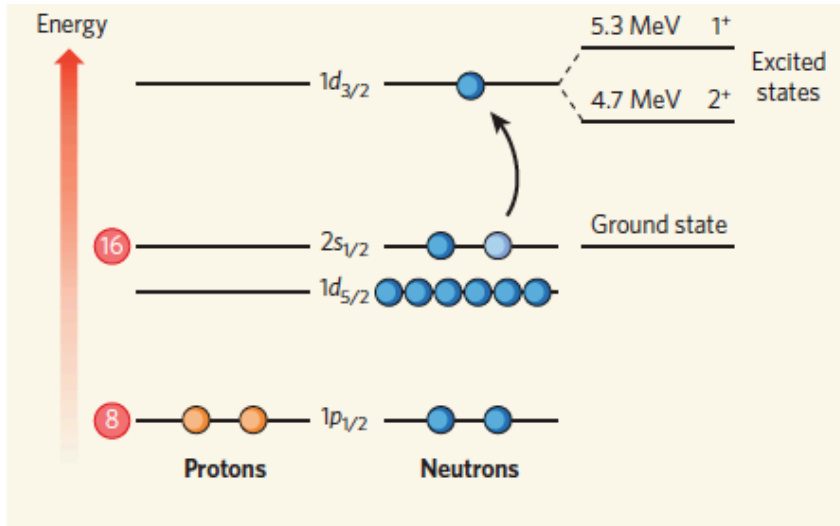
$^{24}\text{O}(p,p')$

# Unexpected doubly magic nucleus

Robert V. F. Janssens

# $^{24}\text{O}$

NATURE -- Vol 459 -- 25 June 2009

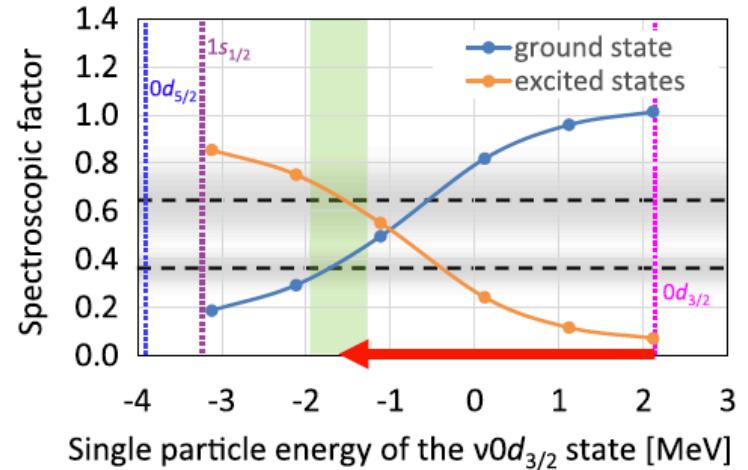
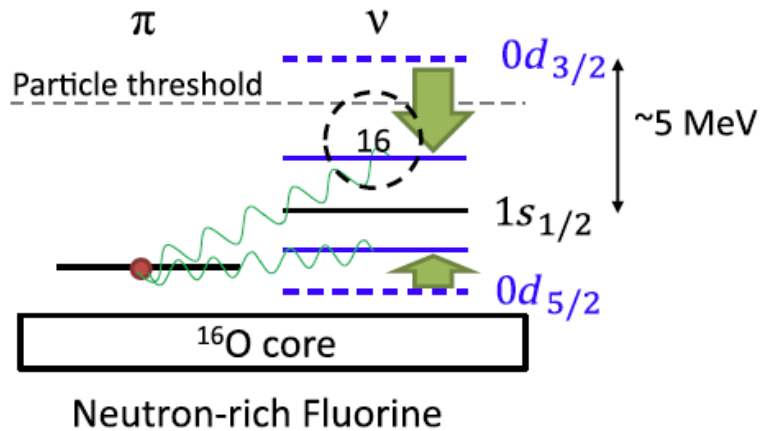


PRL 109, 022501 (2012)

The structure of a neutron-rich  $^{25}\text{F}$  nucleus is investigated by a quasifree ( $p, 2p$ ) knockout reaction at 270A MeV in inverse kinematics. The sum of spectroscopic factors of  $\pi 0d_{5/2}$  orbital is found to be  $1.0 \pm 0.3$ . However, the spectroscopic factor with residual  $^{24}\text{O}$  nucleus being in the ground state is found to be only  $0.36 \pm 0.13$ , while those in the excited state is  $0.65 \pm 0.25$ . The result shows that the  $^{24}\text{O}$  core of  $^{25}\text{F}$  nucleus significantly differs from a free  $^{24}\text{O}$  nucleus, and the core consists of  $\sim 35\%$   $^{24}\text{O}_{\text{g.s.}}$  and  $\sim 65\%$  excited  $^{24}\text{O}$ . The result may infer that the addition of the  $0d_{5/2}$  proton considerably changes neutron structure in  $^{25}\text{F}$  from that in  $^{24}\text{O}$ , which could be a possible mechanism responsible for the oxygen dripline anomaly.

TABLE I. Experimental results, integrated cross-sections, and spectroscopic factors.  $S_{\text{exp}}$  extracted from experimental cross section and theoretical single-particle cross sections.  $J_{\text{th}}^{\pi}$  is the spin-parity used for theoretical calculations.

Channel	Mean [MeV]	Width [MeV]	$\sigma_{\text{exp}} [\mu\text{b}]$	$\sigma_{\text{th}} [\mu\text{b}]$	$J_{\text{th}}^{\pi}$	$S_{\text{exp}}$	$S_{\text{th}}(\text{USDB})$	$S_{\text{th}}(\text{SFO})$	$S_{\text{th}}(\text{SPDF-MU})$
$(^{25}\text{F}, ^{24}\text{O})$	-0.5(1.1)	4.8(1.3)	53(18)	149(24)	$5/2^{+}$	0.36(13)	1.01	0.90	0.95
$(^{25}\text{F}, ^{23}\text{O})$	6.5(1.4)	6.3(9)	81(26)	125(26)	$5/2^{+}$	0.65(25)	0.01	0.07	0.05
$(^{25}\text{F}, ^{22}\text{O})$	12.7(6)	7.6(6)	274(71)	80(24)	$1/2^{-}$	3.43(1.4)		2.19	
$(^{23}\text{F}, ^{22}\text{O})$	1.0(8)	6.0(6)	61(14)	166(28)	$5/2^{+}$	0.37(10)	1.08	0.92	1.00
$(^{23}\text{F}, ^{21}\text{O})$	9.5(4)	7.9(4)	456(67)	93(25)	$1/2^{-}, 3/2^{-}$	4.9(1.5)		5.21	
$(^{23}\text{F}, ^{20}\text{O})$	18.0(5)	9.7(5)							

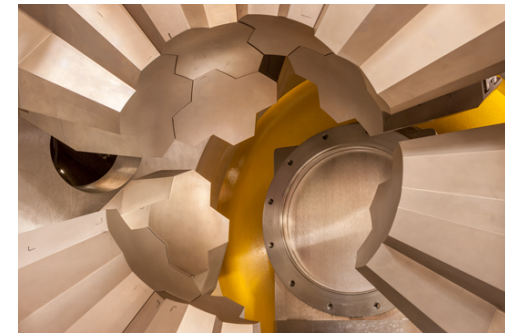
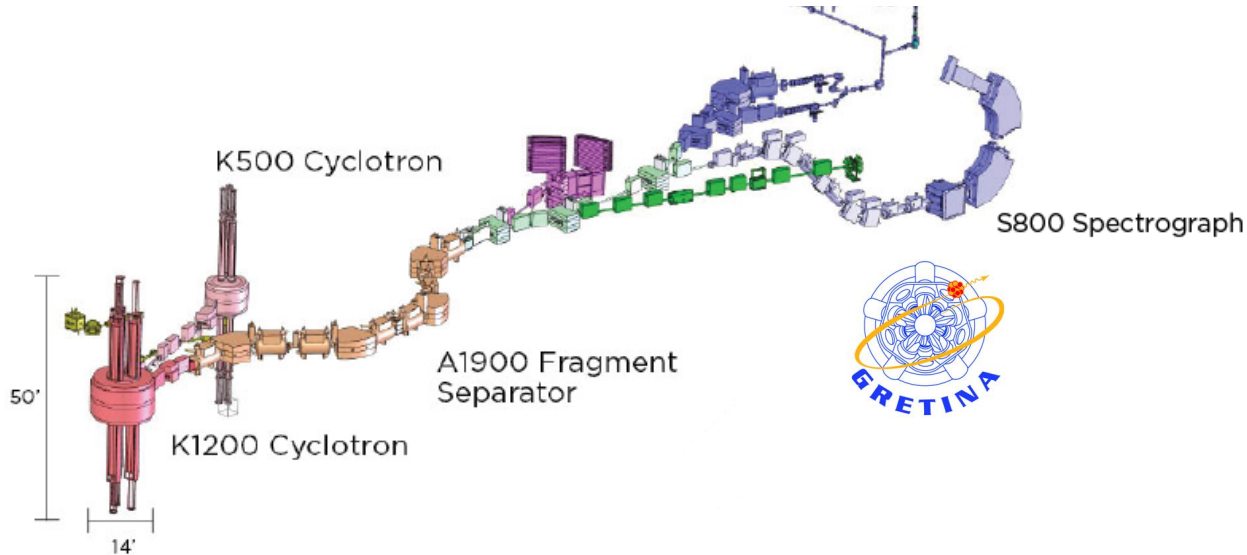
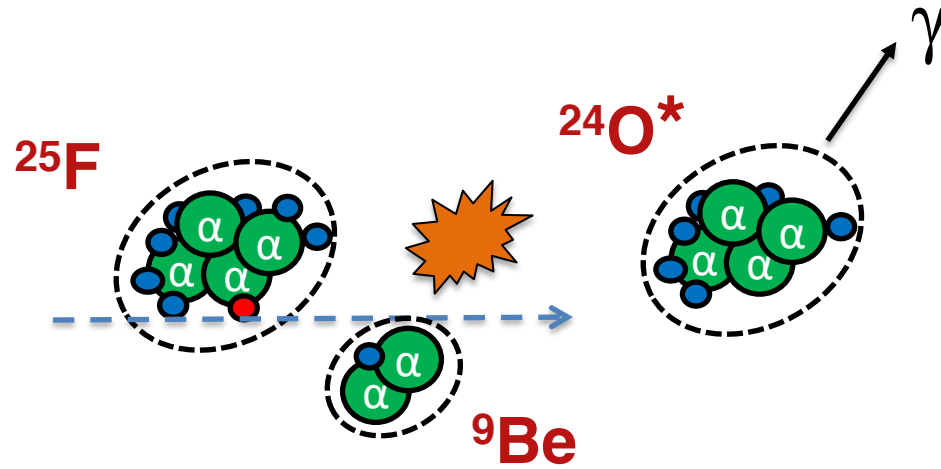


The  $0d_{5/2}$  proton knockout from  $^{25}\text{F}$  populates the  $^{24}\text{O}$  ground state with a smaller probability than the  $^{24}\text{O}$  excited states. This result indicates that the oxygen core of  $^{25}\text{F}$  is considerably different from  $^{24}\text{O}_{\text{gs}}$  and has a larger overlap with the excited states of  $^{24}\text{O}$ . The change in the neutron-shell structure due to the  $0d_{5/2}$  proton may be responsible for the small overlap between  $^{25}\text{F}$  and  $^{24}\text{O}_{\text{gs}}$ .

A comparison with the shell model calculations indicates that the USDB, SFO, and SFPD-MU interactions are insufficient to reproduce the present results. A stronger tensor force or other mechanism such as the 3N force effects, or both, might be needed to explain the experimental results. **More experimental and theoretical studies are necessary to clarify the mechanism for the change in the core of neutron-rich fluorine from the ground state of oxygen isotopes.**

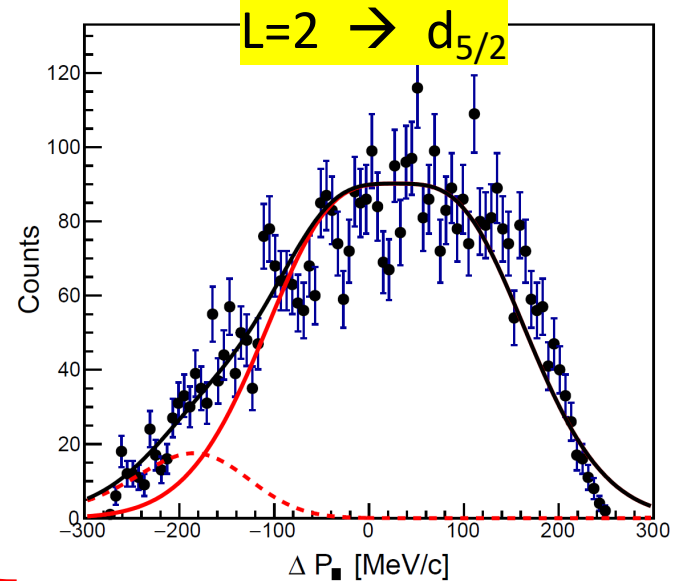
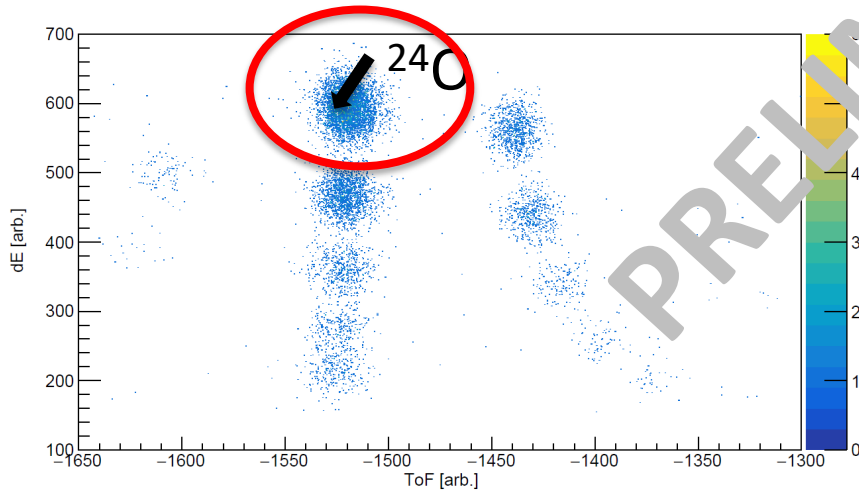
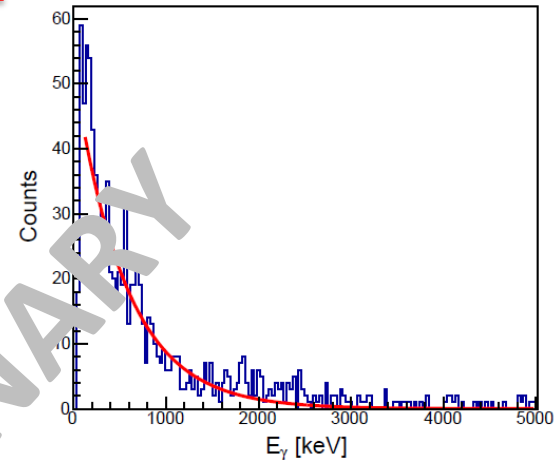
# Proton Knockout at NSCL

E16022: M.D. Jones, H. L. Crawford, *et al.*



# Proton Knockout at NSCL

<sup>20</sup> Ne	<sup>21</sup> Ne	<sup>22</sup> Ne	<sup>23</sup> Ne	<sup>24</sup> Ne	<sup>25</sup> Ne	<sup>26</sup> Ne	<sup>27</sup> Ne
<sup>19</sup> F	<sup>20</sup> F	<sup>21</sup> F	<sup>22</sup> F	<sup>23</sup> F	<sup>24</sup> F	<sup>25</sup> F	<sup>26</sup> F
<sup>18</sup> O	<sup>19</sup> O	<sup>20</sup> O	<sup>21</sup> O	<sup>22</sup> O	<sup>23</sup> O	<sup>24</sup> O	<sup>25</sup> O
<sup>17</sup> N	<sup>18</sup> N	<sup>19</sup> N	<sup>20</sup> N	<sup>21</sup> N	<sup>22</sup> N	<sup>23</sup> N	<sup>24</sup> N



$$\sigma = 5.14 \text{ mb}$$

$$\sigma_{sp} = 17 \text{ mb}$$




$$S = 0.30 (5)$$

PHYSICAL REVIEW C **102**, 041301(R) (2020)

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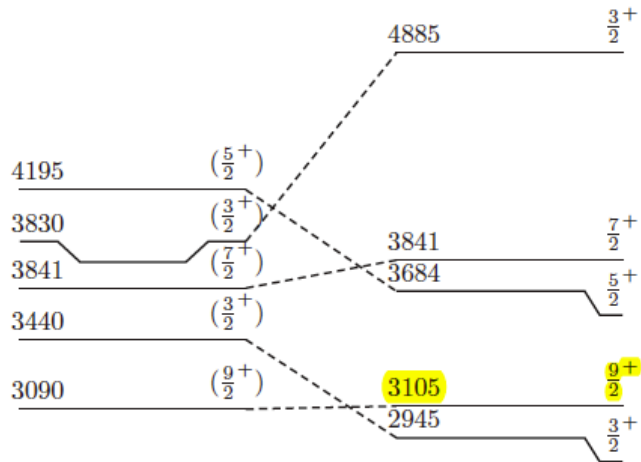
Rapid Communications

### Core of $^{25}\text{F}$ in the rotational model

A. O. Macchiavelli , R. M. Clark, H. L. Crawford, P. Fallon, I. Y. Lee , C. Morse, C. M. Campbell,  
M. Cromaz, and C. Santamaria 

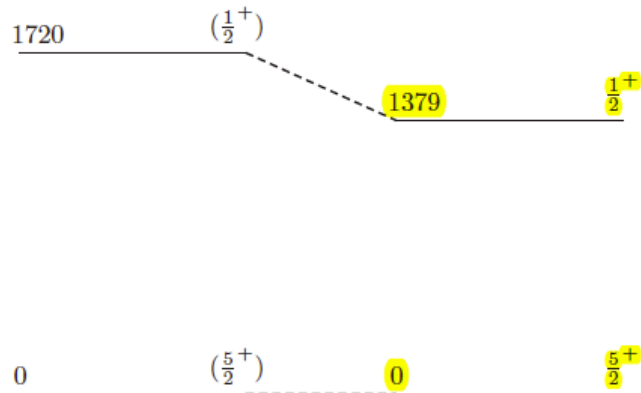
*Nuclear Science Division, Lawrence Berkeley National Laboratory, Berkeley, California 94720, USA*

# $^{25}\text{F}$ in the PRM



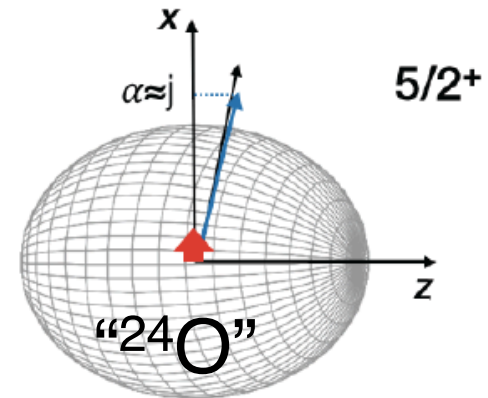
The effective  $^{24}\text{O}$  core in  $^{25}\text{F}$  can be interpreted as a slightly deformed rotor with:

$$E_2^+(\text{core}) \approx 3.2 \text{ MeV and } \mathcal{E}_2 \approx 0.15,$$

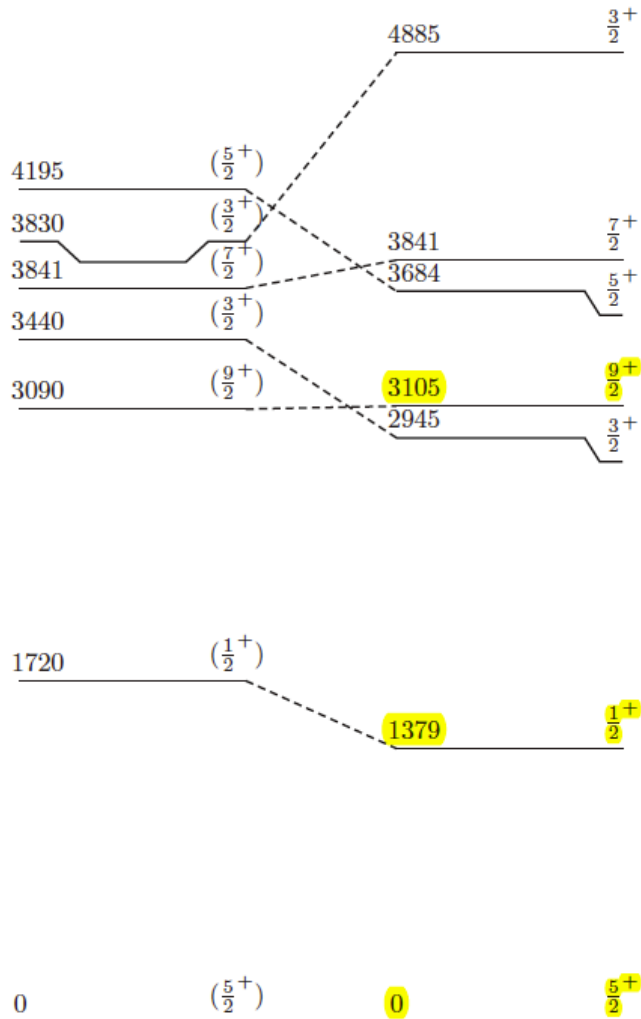


Experiment

Theory



# $^{25}\text{F}$ in the PRM



Furthermore, in  $^{26}\text{F}$  \* the  $1^+$  ground and  $4^+$  isomeric states can be associated with the antiparallel and parallel couplings of the odd neutron in the  $d_{3/2}$  Nilsson multiplet to the structure of  $^{25}\text{F}$ .

The former, favored by the Gallagher-Moszkowski rule gives  $1^+$  as the lowest state and the latter a  $4^+$  as the bandhead of a doubly decoupled band.

\* A. Lepailleur *et al.*, *Phys. Rev. Lett.* **110**, 082502 (2013)

Experiment

Theory

# Spectroscopic factors

PRM



$$\psi_I = \sum_K \mathcal{A}_K |IK\rangle.$$



$$S_{i,f}(j\ell) = \left( \sum_K \mathcal{A}_K \theta_{i,f}(j\ell, K) \right)^2,$$

$$\theta_{i,f}(j\ell, K) = \sqrt{2} \langle I_i j K \Omega_\pi | I_f 0 \rangle C_{j,\ell} \langle \phi_f | \phi_i \rangle$$

Nilsson amplitudes



Core overlap



# Spectroscopic factors

Final state in $^{24}\text{O}$	$S_{\text{exp}}$ Ref. [7]	$S_{\text{th}}$		
		PRM1	PRM2	SDPF-MU
Ground	0.36(13)	0.85	0.56	0.95
Excited	0.65(25)	0.15	0.44	0.05

$$\langle \phi_f | \phi_i \rangle \approx 0.81^*$$

Following: T. Takemasa, M. Sakagami, and M. Sano, Phys. Rev. Lett. **29**, 133 (1979).  
T. Takemasa, Comput. Phys. Commun. **36**, 79 (1985).

\*\*Not Quenching ??

\* | A simple volume overlap gives  $\langle \phi_f | \phi_i \rangle \approx \frac{1}{1 + \epsilon_2 + \frac{2}{3}\epsilon_2^2 + \dots} \approx 0.85$ .

# Further studies ?

TABLE II. Electromagnetic properties of the low-lying levels of  $^{25}\text{F}$  in the PRM. Magnetic moments have been calculated using  $g_R = Z/A$  and  $g_s = 0.7(g_s)_{\text{free}}$ .

$I^\pi$	$E_x$ (MeV)	$\mu$ ( $\mu_N$ )	$Q$ ( $efm^2$ )	$B(E2; I \rightarrow \frac{5}{2}^+)$ (WU)
$\frac{5}{2}^+$	0	3.9	-4.5	
$\frac{1}{2}^+$	1.4	1.9	0	3.9
$\frac{9}{2}^+$	3.1	4.6	-7.8	1.9

# Summary and conclusions

The low-lying structure of  $^{25}\text{F}$  can be understood in terms of the rotation-aligned coupling limit of the PRM.

Coriolis coupling on the  $d_{5/2}$  proton Nilsson multiplet gives rise to a decoupled band with a  $5/2^+$  bandhead.

Calculated proton spectroscopic factors for the  $^{25}\text{F}(5/2^+)(-1p) ^{24}\text{O}$  reaction are in agreement with the experimental data. The observed fragmentation of the  $d_{5/2}$  strength is due to both deformation and a core overlap.

The Nilsson plus PRM picture suggests that the extra proton with a dominant component in the down-sloping  $[220] \frac{1}{2}$  level polarizes  $^{24}\text{O}$  and stabilizes its dynamic deformation. Thus, the effective core in  $^{25}\text{F}$  can be interpreted as a slightly deformed rotor with  $E2^+$  (core)  $\approx 3.2$  MeV and  $\varepsilon_2 \approx 0.15$ , compared to the real doubly magic  $^{24}\text{O}$  with  $E2^+ \approx 4.7$  MeV and weak vibrational quadrupole collectivity.

Electromagnetic observables for the three lowest experimental levels, obtained in the PRM, suggest that measurements of the magnetic and quadrupole moments of the  $5/2^+$  state as well as Coulomb excitation will shed further light on the validity of our interpretation.

**Thank You !**